

# Curvature-based Analysis of Network Connectivity in Private Backbone Infrastructures

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# Cloud Providers are investing billions \$ in their backbones

TECH | KEYWORDS: CHRISTOPHER MIMS

## Google, Amazon, Meta and Microsoft Weave a Fiber-Optic Web of Power

The four tech giants increasingly dominate the internet's critical cable infrastructure

TELECOM

## Google to build 3 submarine cables to battle Microsoft, AWS for cloud customers

By Sean Buckley • Jan 16, 2018 10:19am

## Microsoft, Facebook and Telxius complete the highest-capacity subsea cable to cross the Atlantic

People and organizations rely on global networks every day to provide access to internet and cloud technology. Those systems enable tasks both simple and complex, from uploading photos and searching webpages to conducting banking transactions and managing air-travel logistics. Most people are aware of their daily dependency on the internet, but few understand the critical role played by the subsea networks spanning the planet in providing that connectivity.

COMPANIES > AMAZON

## AWS Will Be Google and Facebook's Neighbor on the New US-Europe Submarine Cable

### Press release

AWS Announces Global Expansion of AWS Local Zones

February 16, 2022 at 6:00 PM EST

*Building off the successful launch of AWS Local Zones in 16 US cities, over 30 new AWS Local Zones will deliver single-digit millisecond latency performance at the edge of the cloud to hundreds of millions of people worldwide*

*Netflix, Couchbase, Supercell, and FOX Corporation among thousands of customers using AWS Local Zones*

# Cloud Providers are investing billions \$ in their backbones

## Every cloud deployment is unique

Differences in infrastructure arises in AWS, Azure and GCP through:

- constraints created by geography
- historical infrastructure
- unique strategies and different business goals

Cloud Providers are investing billions \$ in their backbones

Every cloud deployment is unique

How to map the topology: traditional approaches

- Apply bag of heuristics to infer router-level interconnectivity from traceroute measurements
- Geolocate routers with rDNS hints and generate physical topology.

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Already described in **Rocketfuel (Spring *et al.* 2002)** more than 20 years ago!

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***Why does this not work for CP?***

# *Why does this not work for CP?*

Historical challenges

Modern-day challenges

Dependency on the willingness of cloud providers and ISPs to collaborate

## Goals

### **For the academic researcher**

- Getting a clearer view of hardly observable topologies that carry a huge portion of the traffic.
- Comparing and contrasting network properties of the different cloud providers.
- Perspective on a post-traceroute world.

### **For the network engineer at Google**

- Discovering what part of my topology is visible from an outsider perspective
- Monitoring your network with a new visualization of tools



## Starting point:

**Imagine that we have access to devices to schedule measurements and we know where they are (physically) located**

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## Problem:

**We are interested in discovering how they are  
connected to each other**

Measurements  
+ locations



Connectivity  
Network

## Two key ideas:

1. Transferring complexity from measurement to modeling: cast the problem as an instance of manifold learning.
2. Geography as part of the topological representation of the Internet: constrain the manifold to be on the world map.

# Onto the Methodology

1) Measuring the topology

2) Creating graph through  
filtrations

3) Computing Ricci curvature

4) Analysis of the graphs

5) Merging everything into a  
single manifold visual

# What is residual latency?

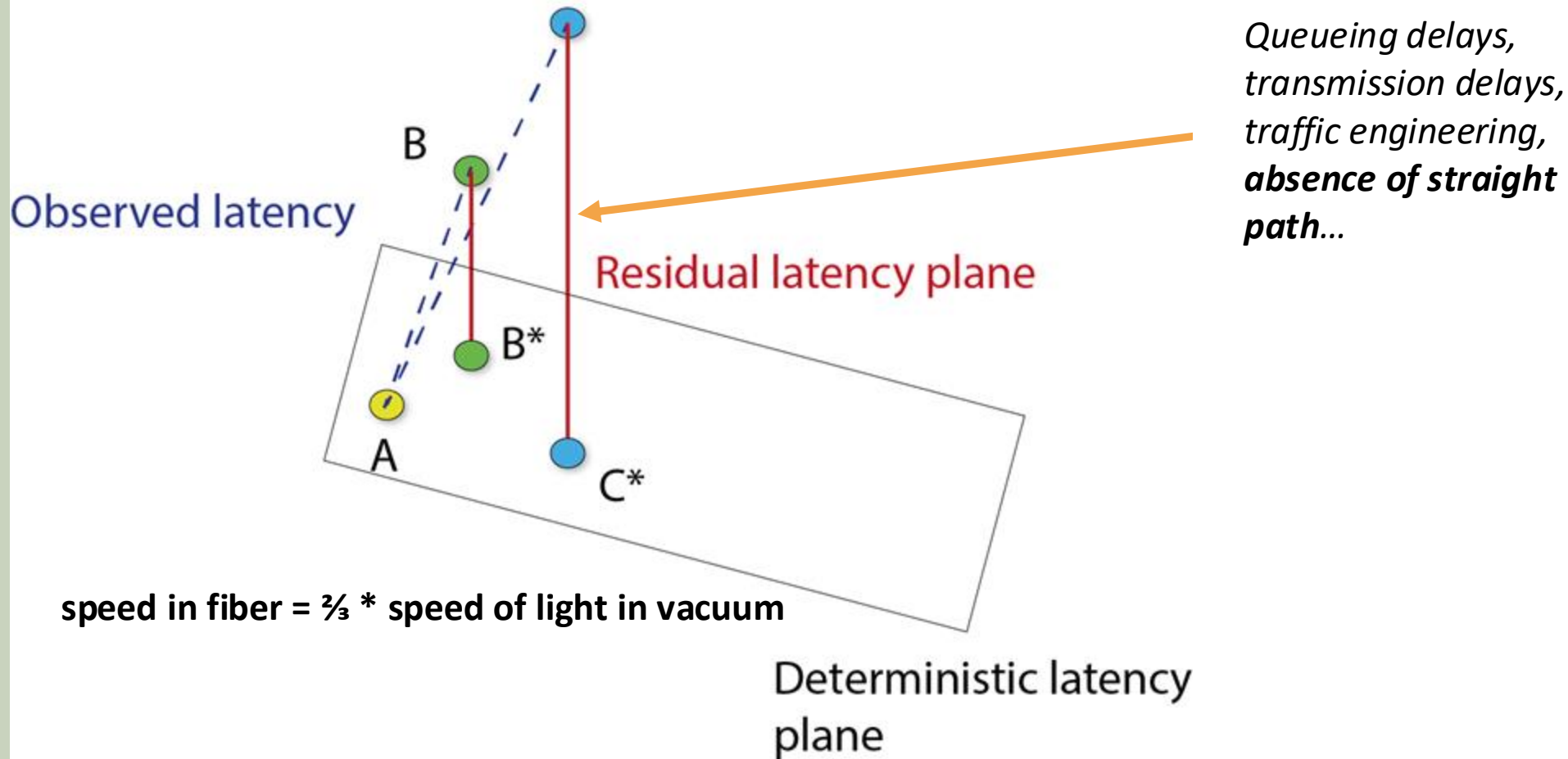
## Deterministic latency



speed in fiber =  $\frac{2}{3}$  \* speed of light in vacuum

# What is residual latency?

We schedule ping measurements



# What is residual latency?

We schedule ping measurements : alternate view

Sampling through a long period of time

$$X(A, B) = \min_{t \in \mathbb{R}} (X_t)(A, B)$$

*Real shortest latency*

*minimize queueing delays*

*minimize transmission delays*

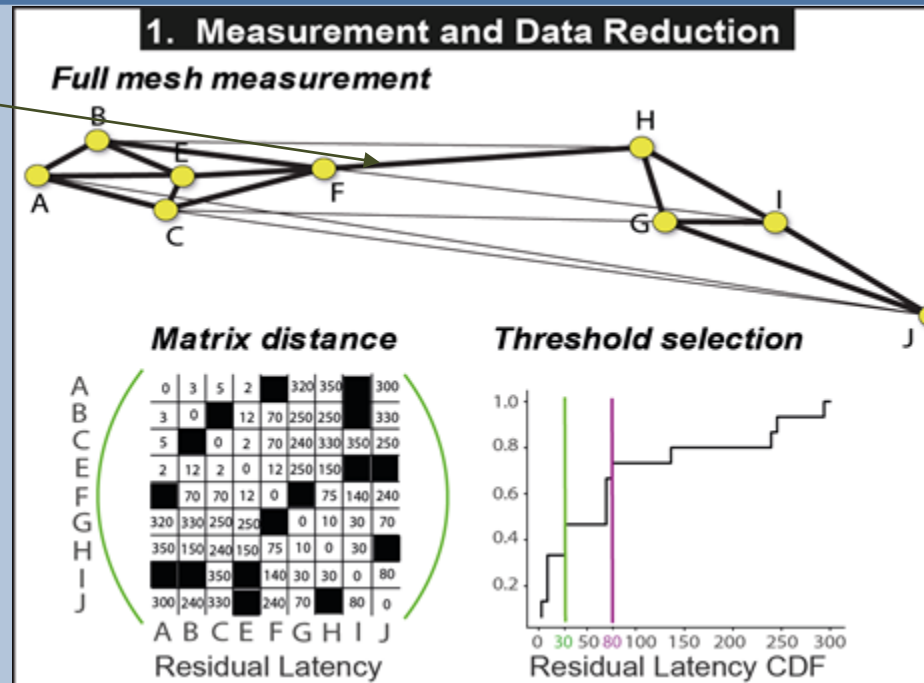
# What is residual latency?

We schedule ping measurements : alternate view

Sampling through a long period of time

Building a *distance* matrix from the residual latency

Real  
fiber





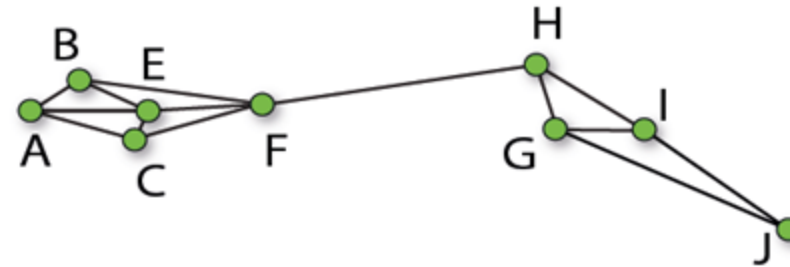
## Building graphs

### 2. Graph Construction

**Small threshold  $\epsilon=30$**

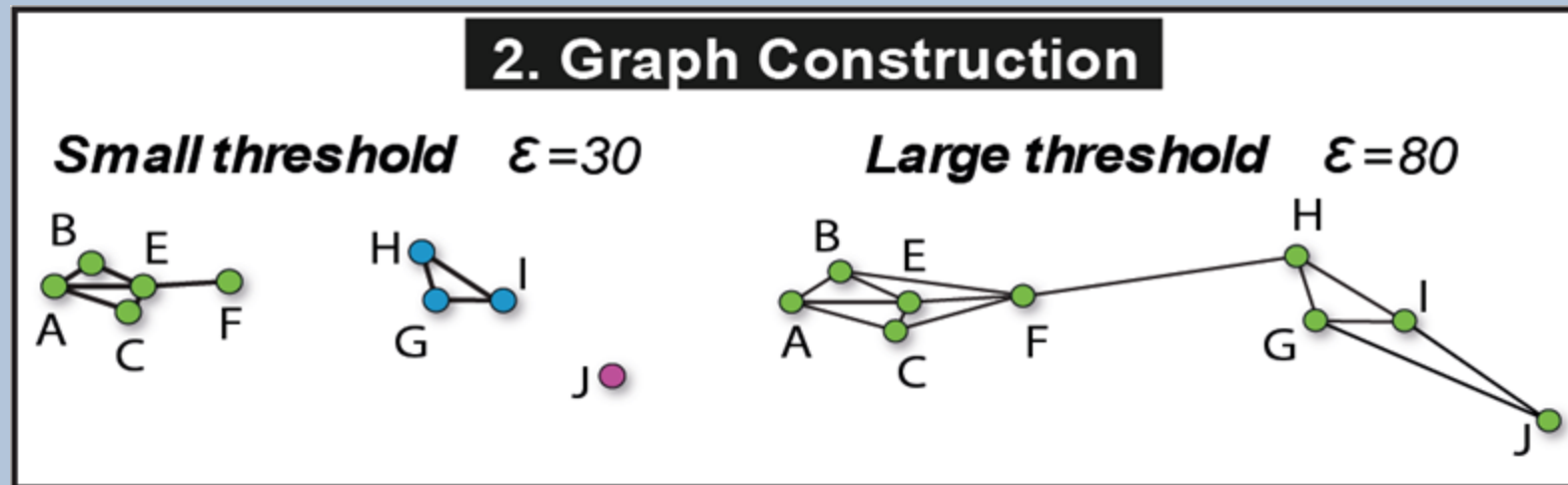


**Large threshold  $\epsilon=80$**



Inspired by Algebraic Topology filtrations

## Building graphs



Inspired by Algebraic Topology filtrations

*How to detect when the real  
topology has been uncovered?*

# Geometrization of graphs

Idea: Leveraging geometric ideas to discover shapes through the discrete Olivier-Ricci curvature

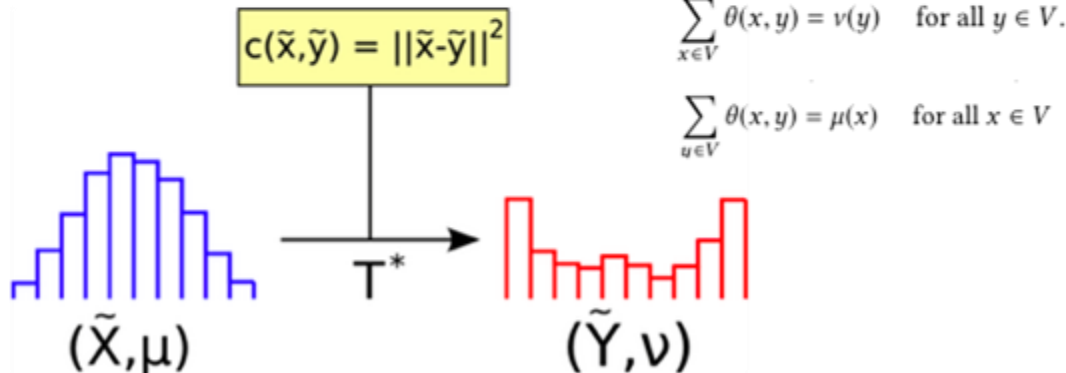
## Optimal Transport Recaps

Evaluate the cost of transferring a specific distribution  $\mu$  of mass on the nodes of a graph to another distribution  $\nu$

Two distributions:  $\sum_x \mu(x) = 1 \quad \sum_x \nu(x) = 1$

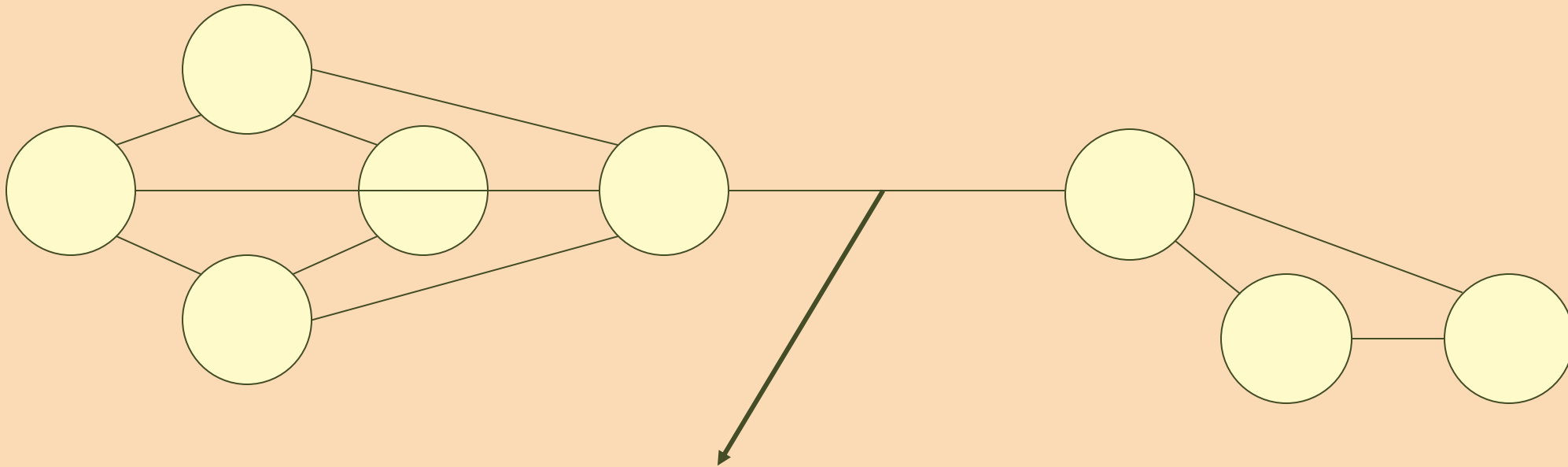
A distance :  $d(x, y)$  or  $c(x, y)$  is the cost of transport one unit of mass, i.e. Euclidean distance, Manhattan distance

Optimal transport:  $\theta^*(\mu, \nu) = \arg \min_{\theta} \sum_{x, y \in V} \theta(x, y) d(x, y)$ , constrained to



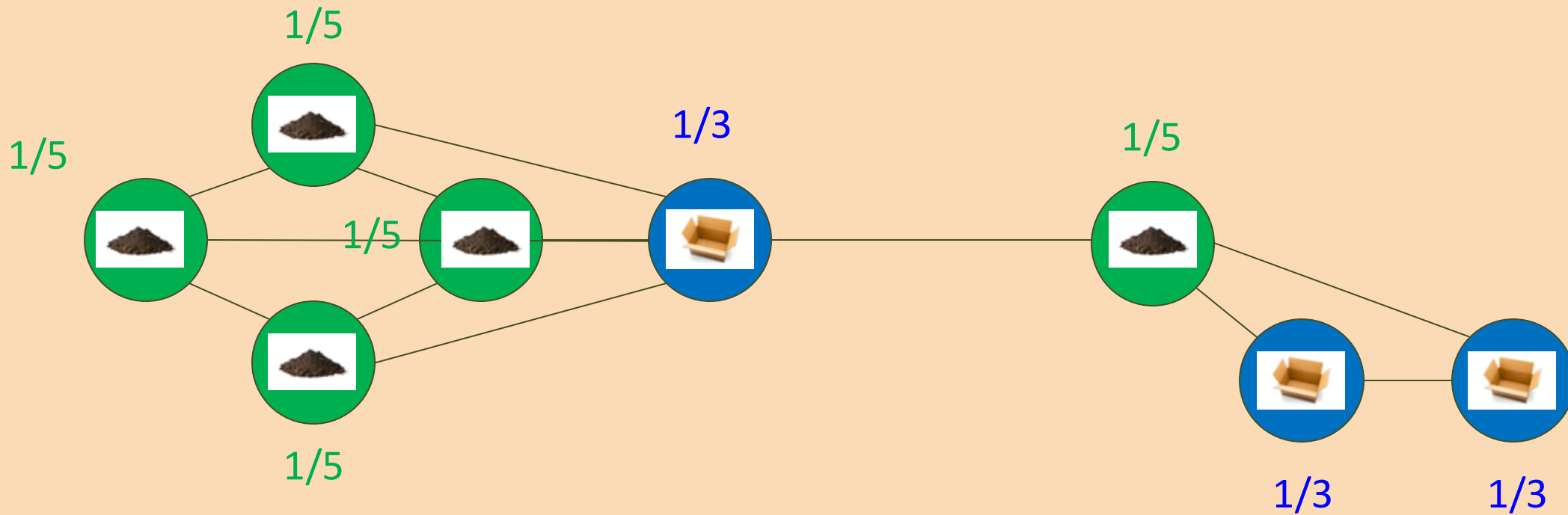
X

## A worked out example

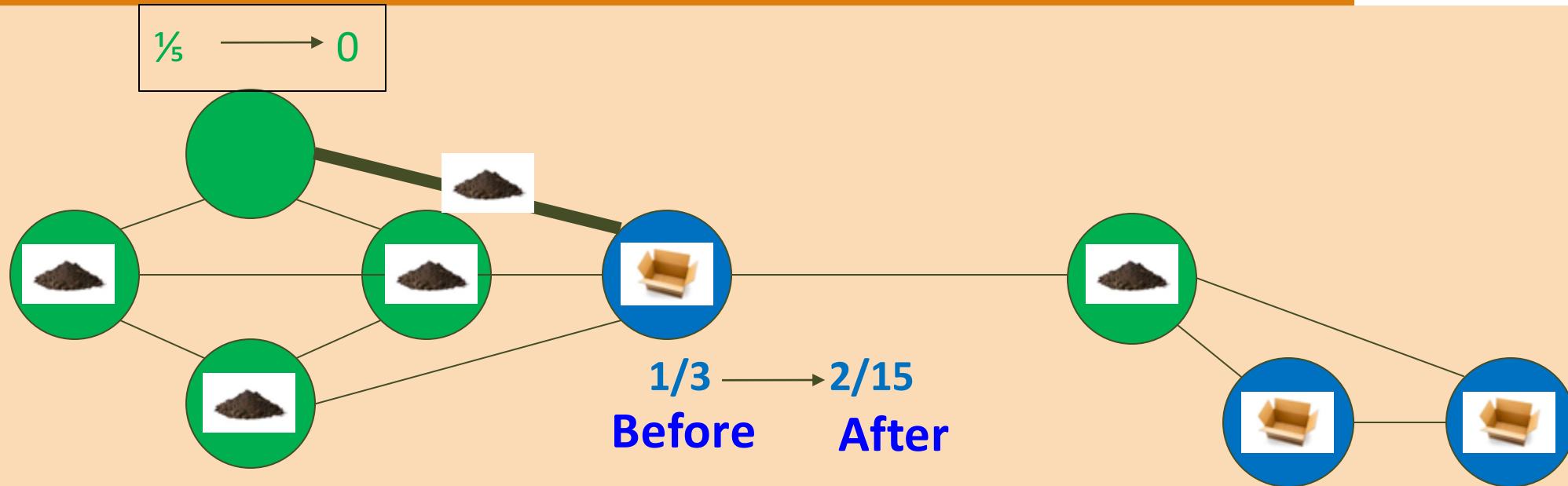


**We are interested in computing the  
optimal transport of this link neighbors**

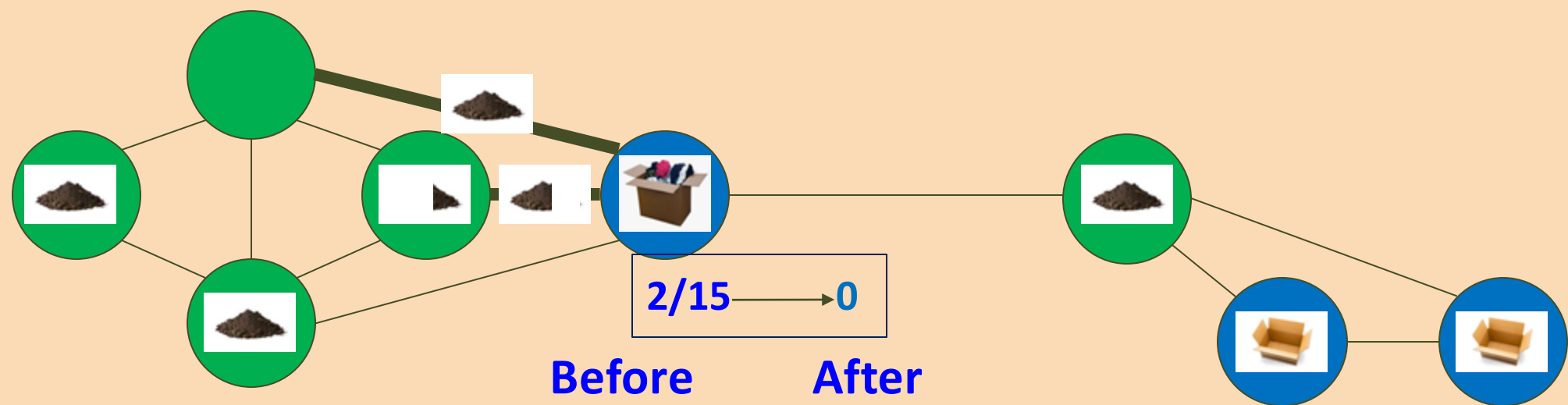
Put dirt on the green nodes and empty boxes on the blue ones



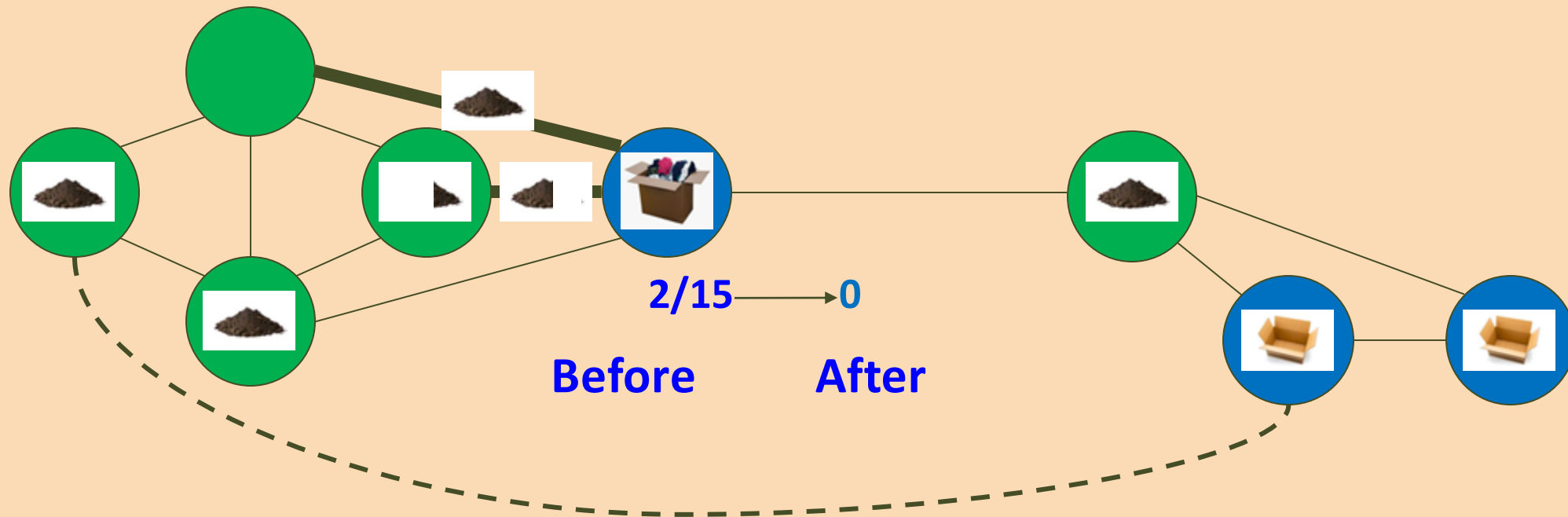
Move the weight from upper node to an empty box



# Filling a box by moving a parcel of dirt



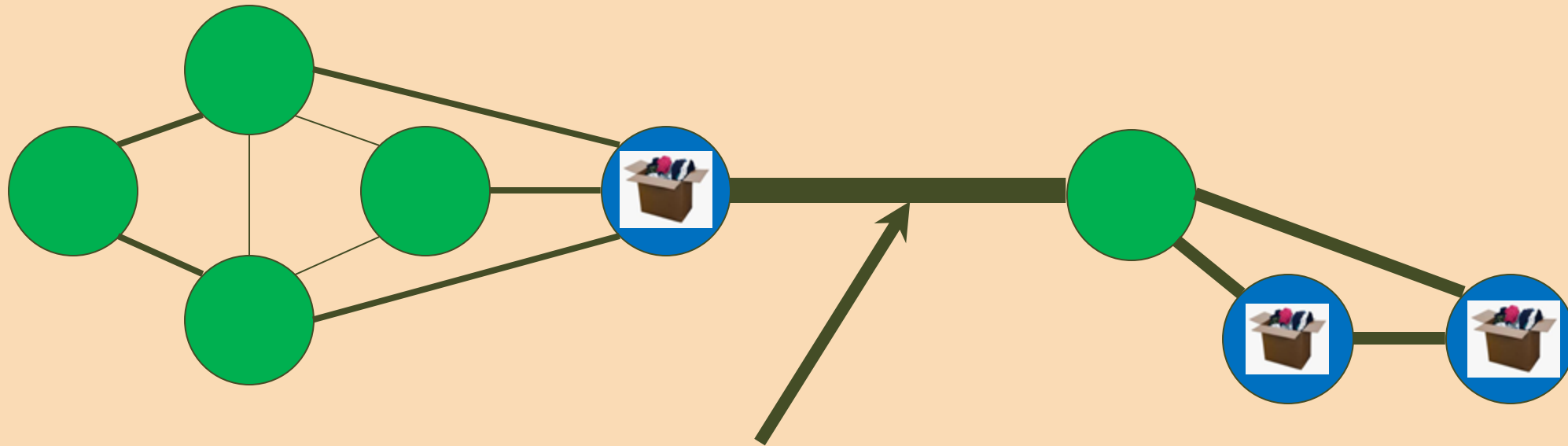
The edge at the middle is a bottleneck



*Only far boxes  
available!*

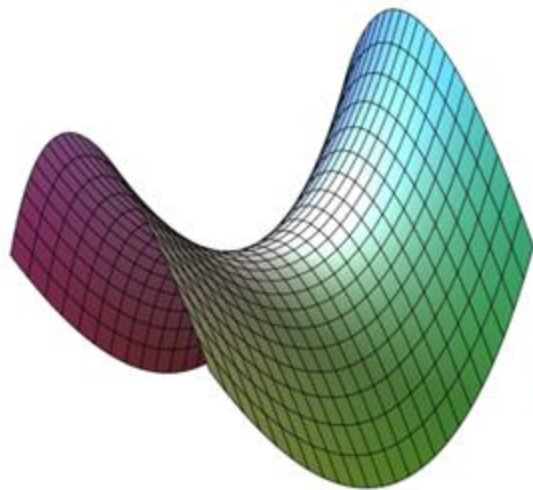


Identifying the edges that have carried a lot of dirt

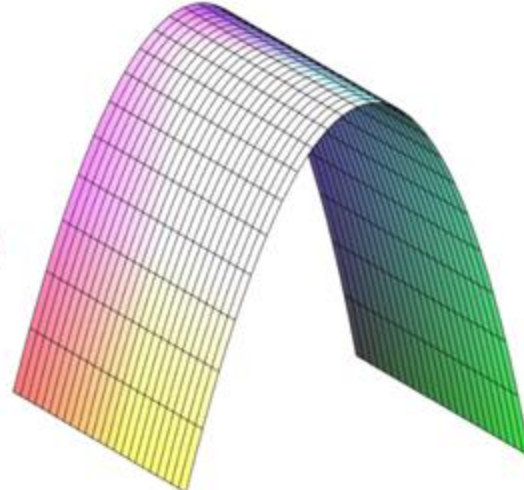


**Lot of the dirts cross this  
edge!**

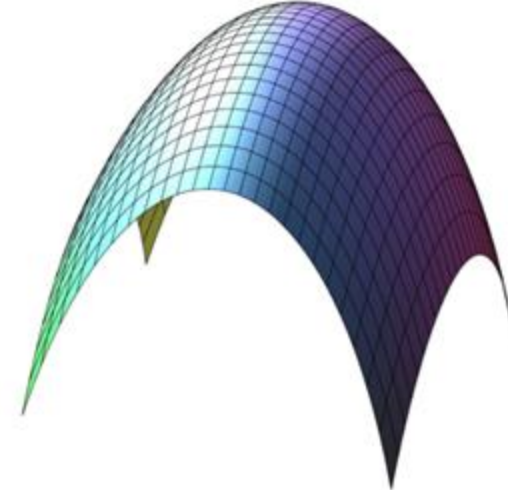
# Continuous and discrete curvature



(a) Surface of Negative Curvature



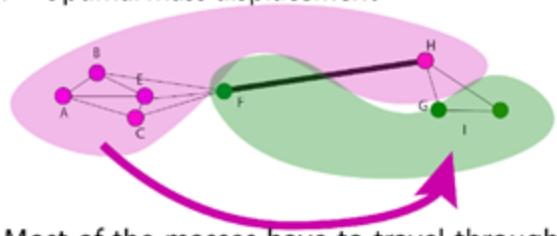
(b) Surface of Zero Curvature



(c) Surface of Positive Curvature

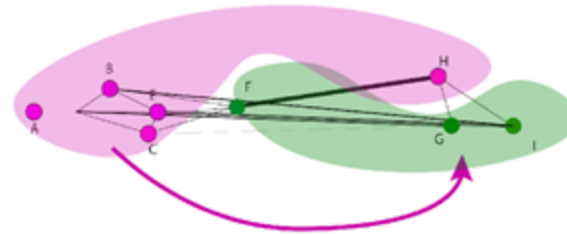
## Negative Curvature

- Distribution  $\mu$
- Distribution  $\nu$
- Optimal mass displacement



Most of the masses have to travel through the edge (FH)

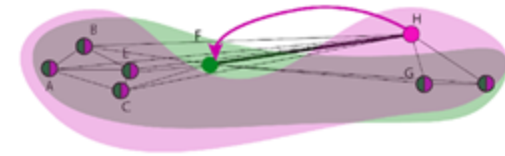
## Neutral Curvature



The neighborhoods are well connected to each other, (FH) is only transiting its own mass

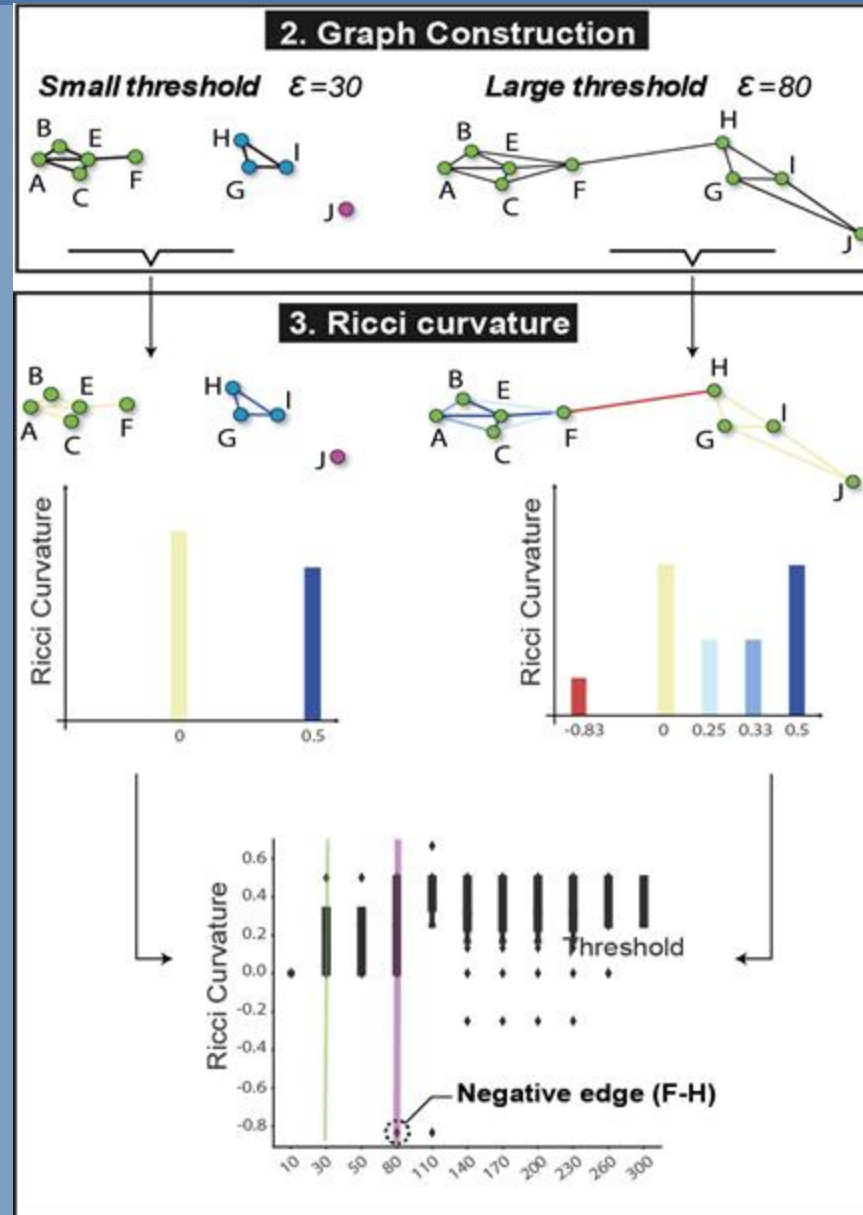
## Positive Curvature

- Distribution  $\mu$  and  $\nu$

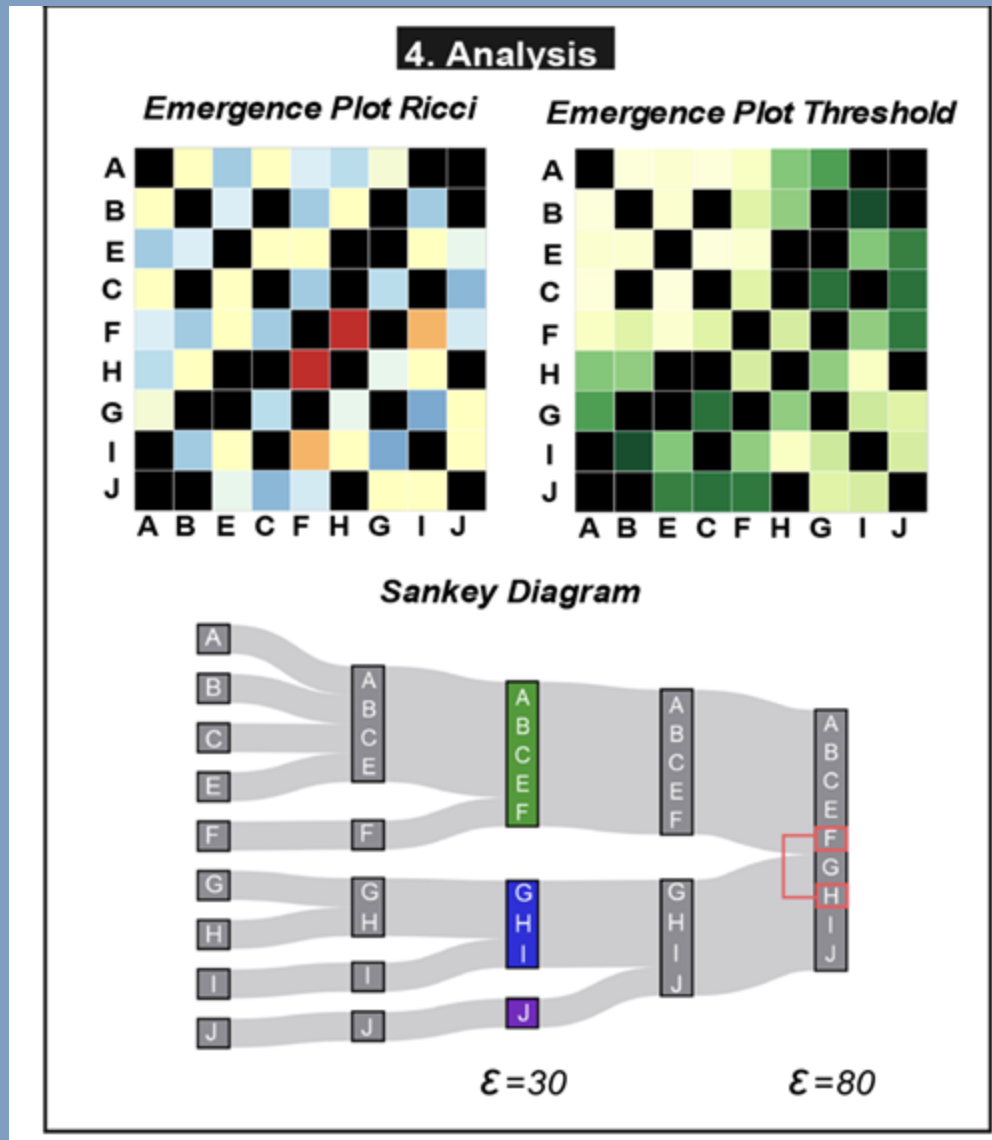


Most of the masses are mingled. The only mass that has to be moved is the one from F to H

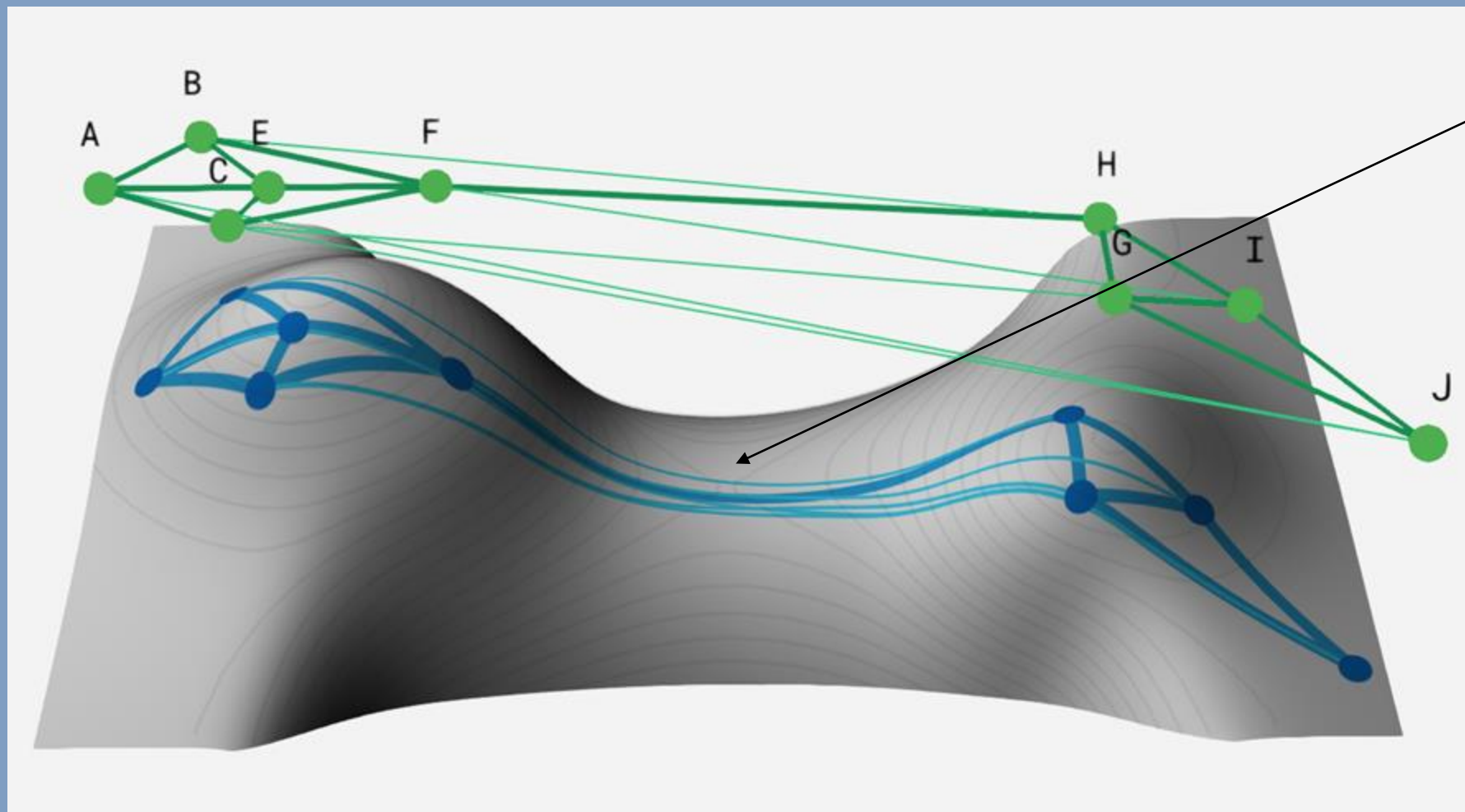
# Negative Ricci curvature matters



# Finding interesting threshold and edges



## Linking back to the continuous view



Geodesic fits  
physical topology

This view exists for each threshold

# Onto the Application

1) Data Collection

2) Building the graphs

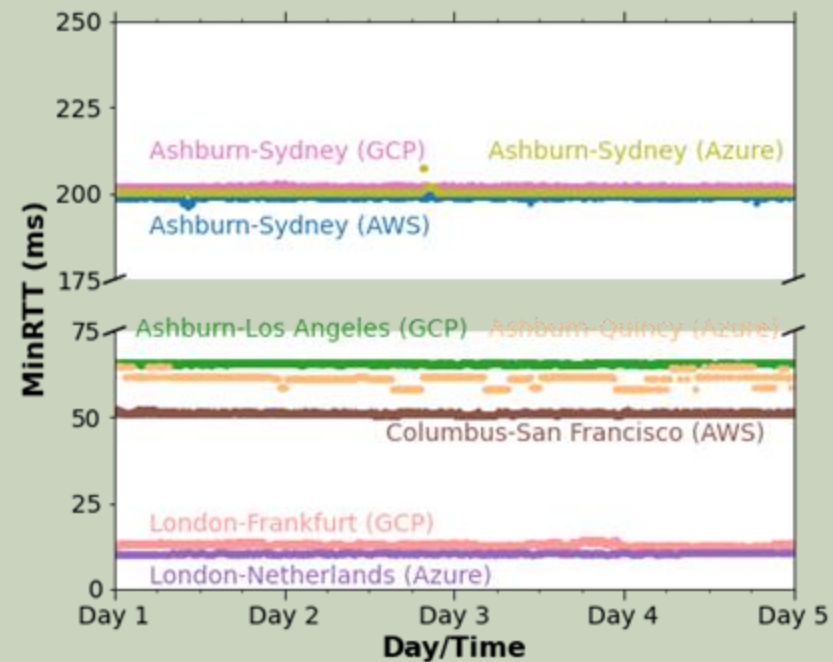
3) Analyzing the manifold

4) Validating the manifold

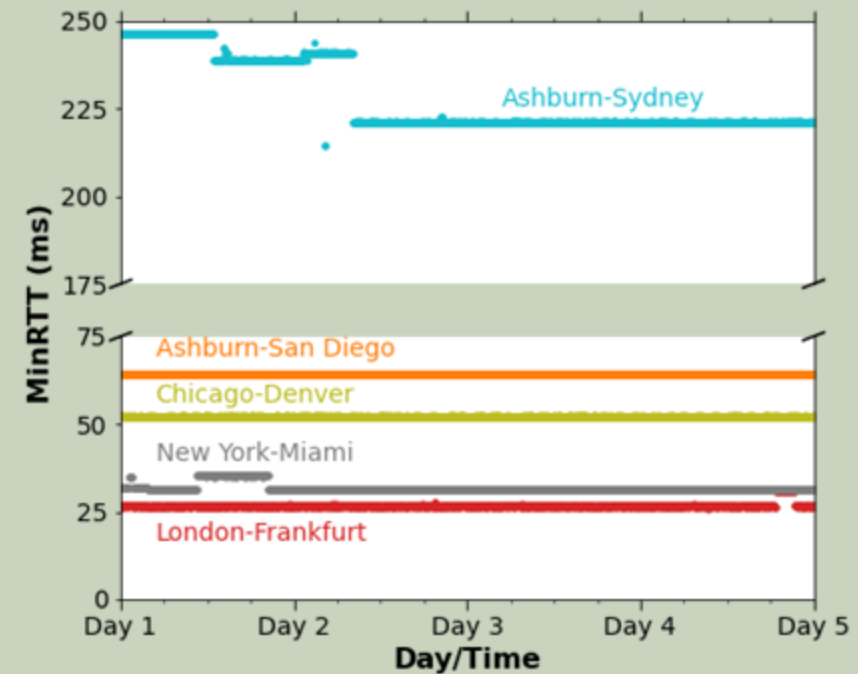
5) Sensitivity analysis

We schedule ping measurements from the different CPs

From the Cloud



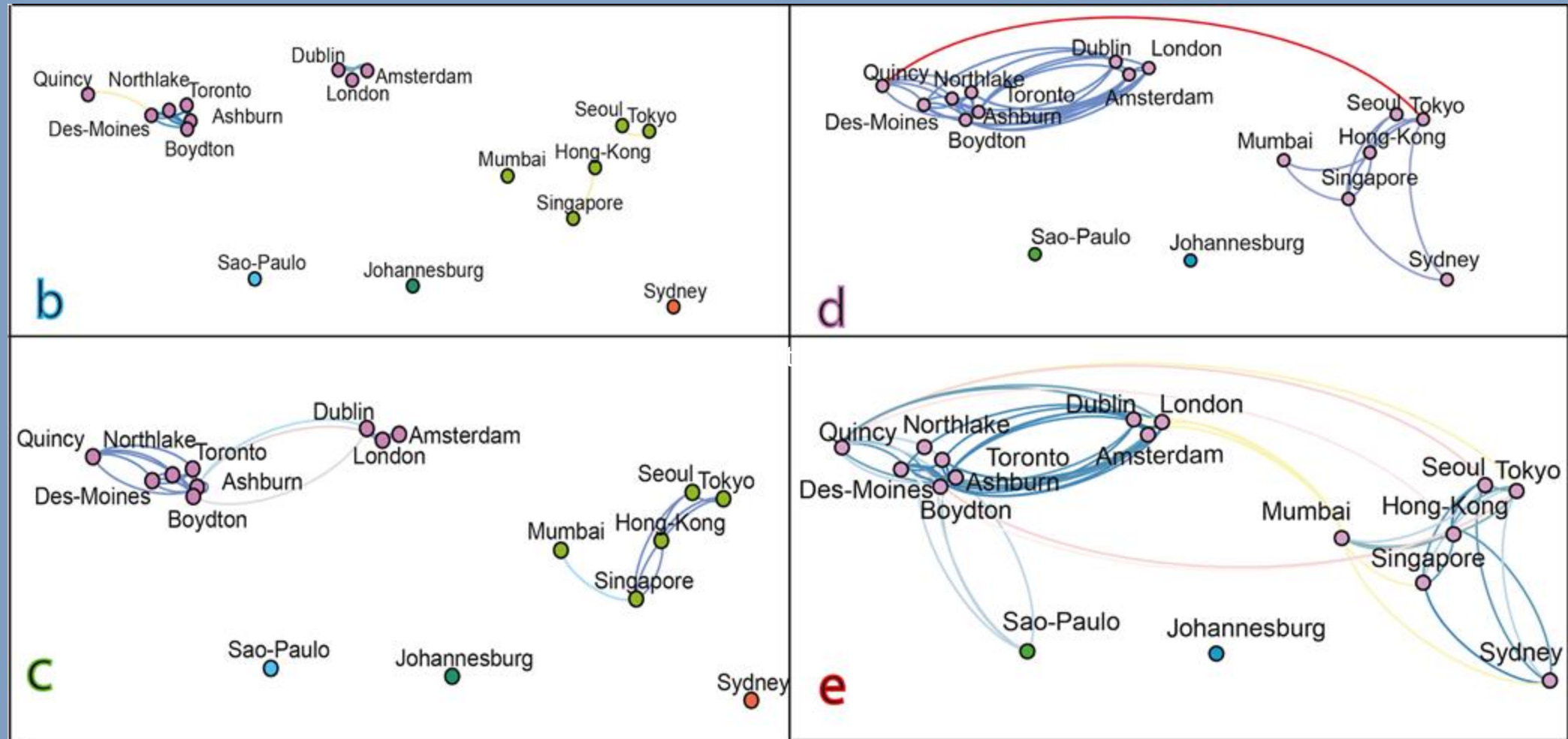
Public Internet in comparison



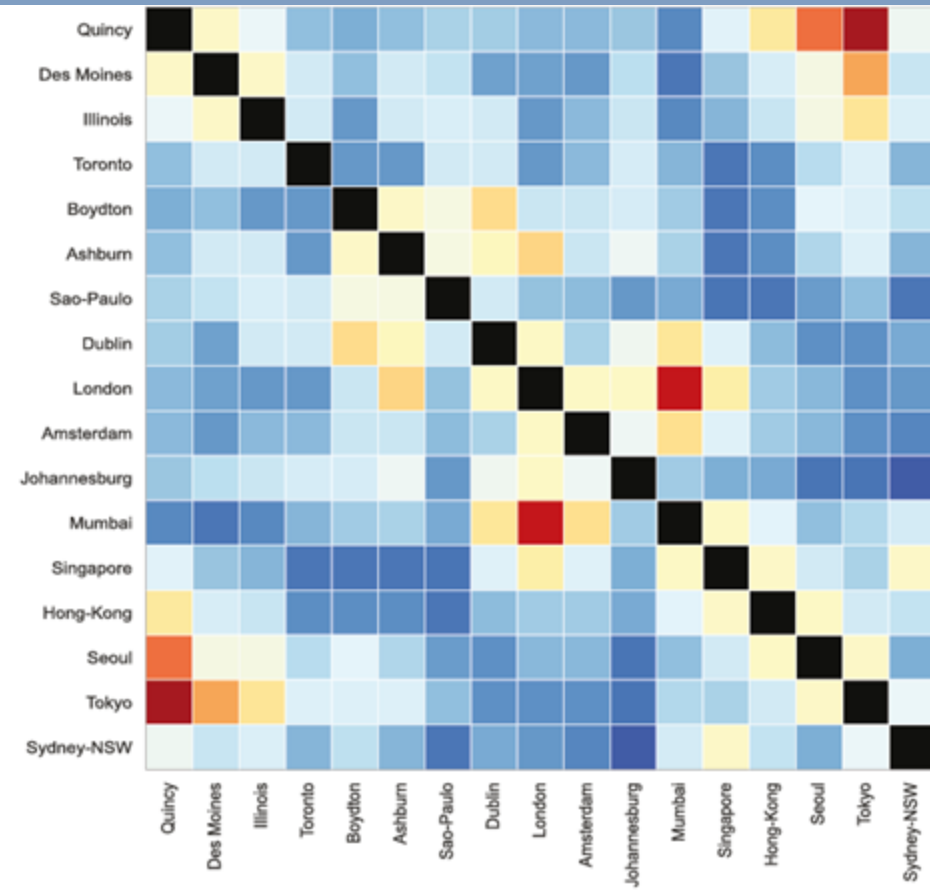
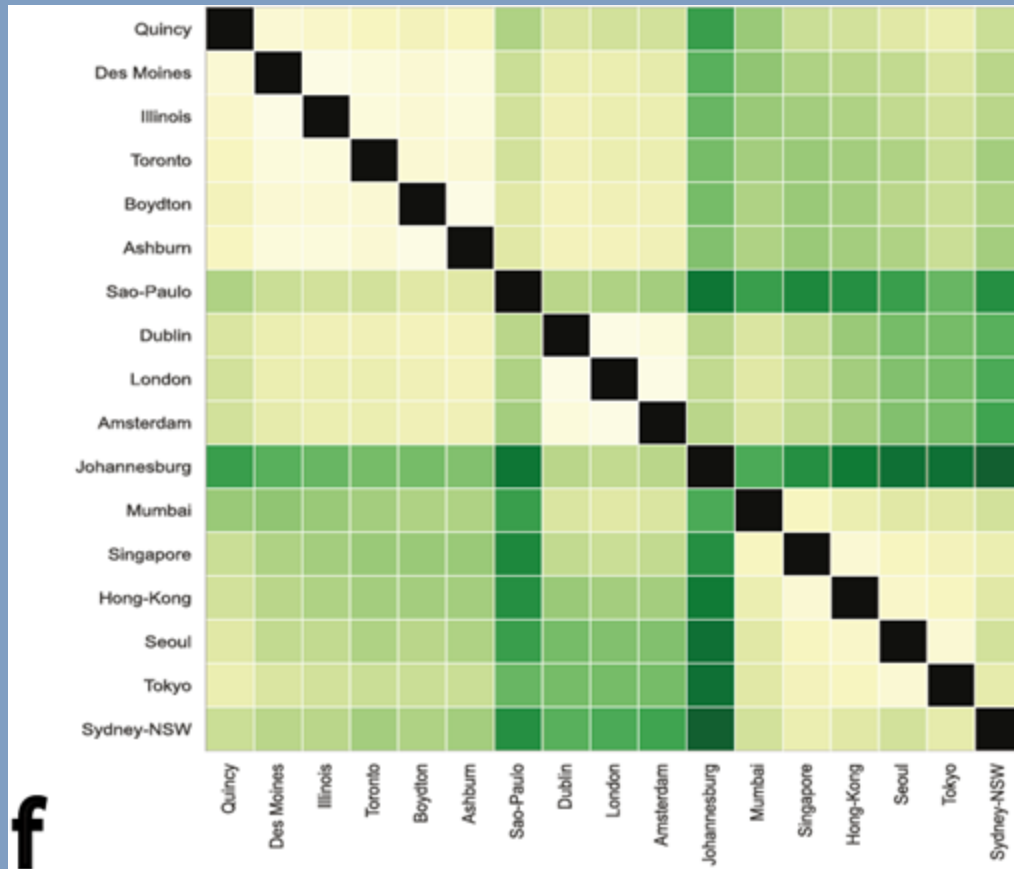




# Building the graphs

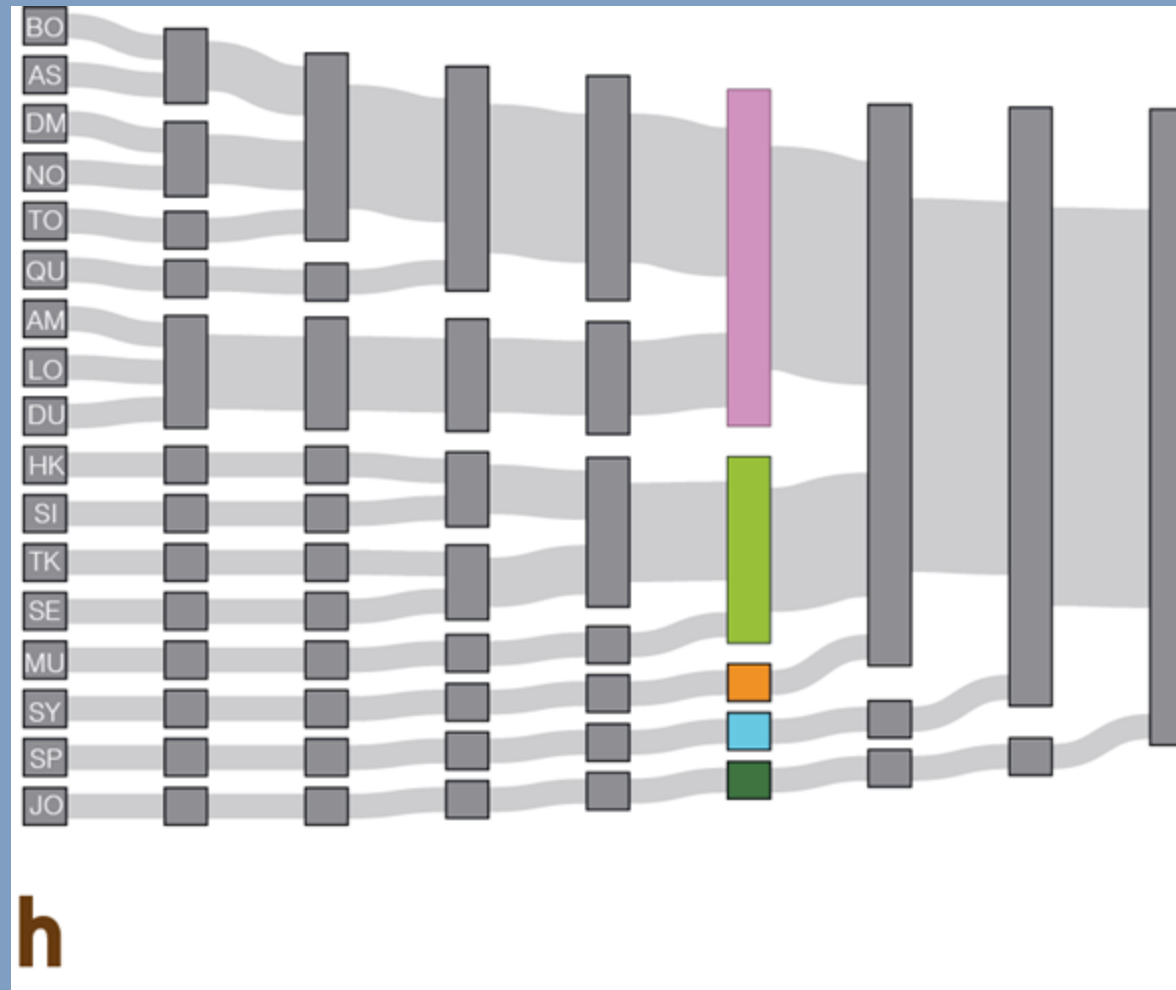


# Aggregating the observation through the heatmaps

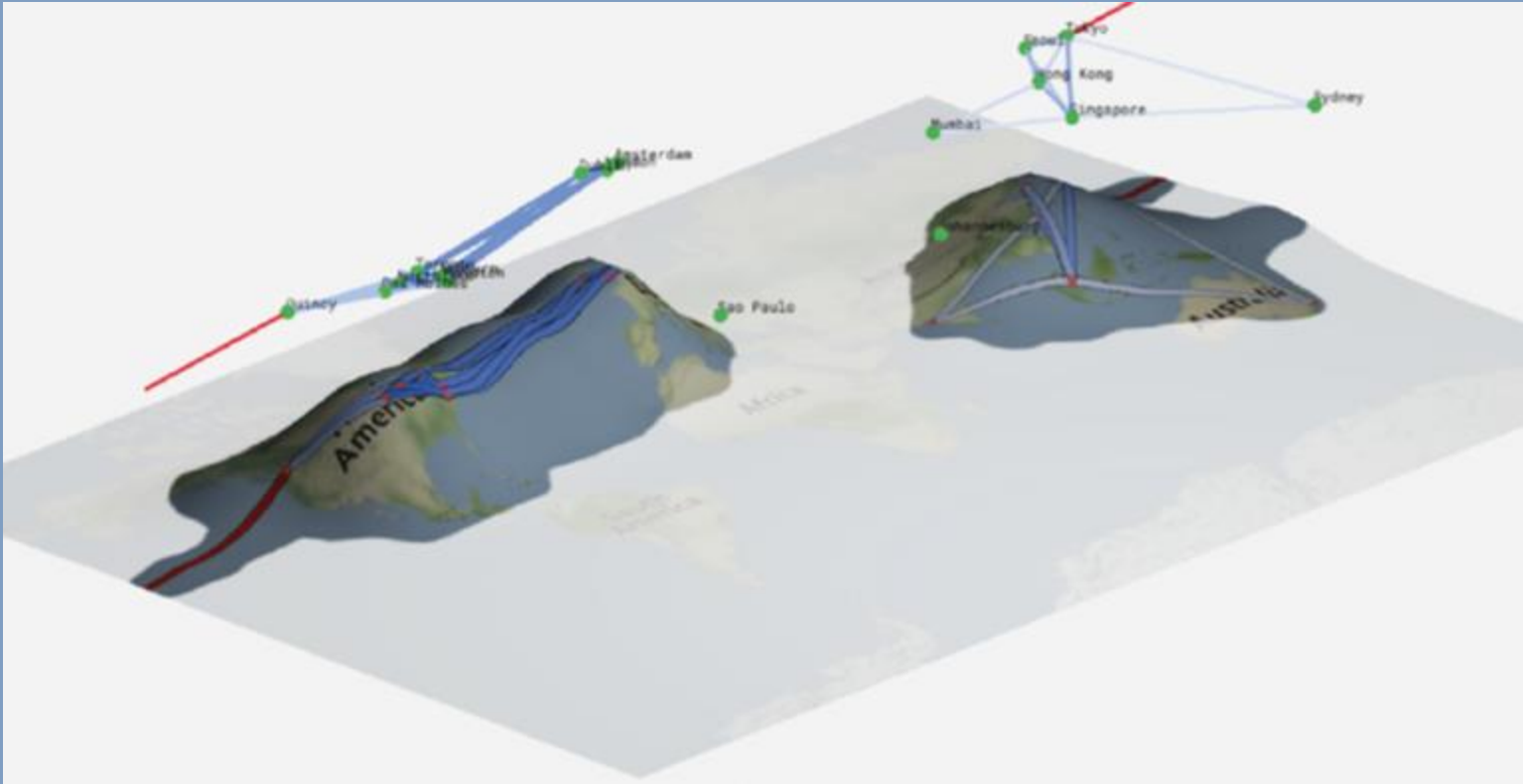


f

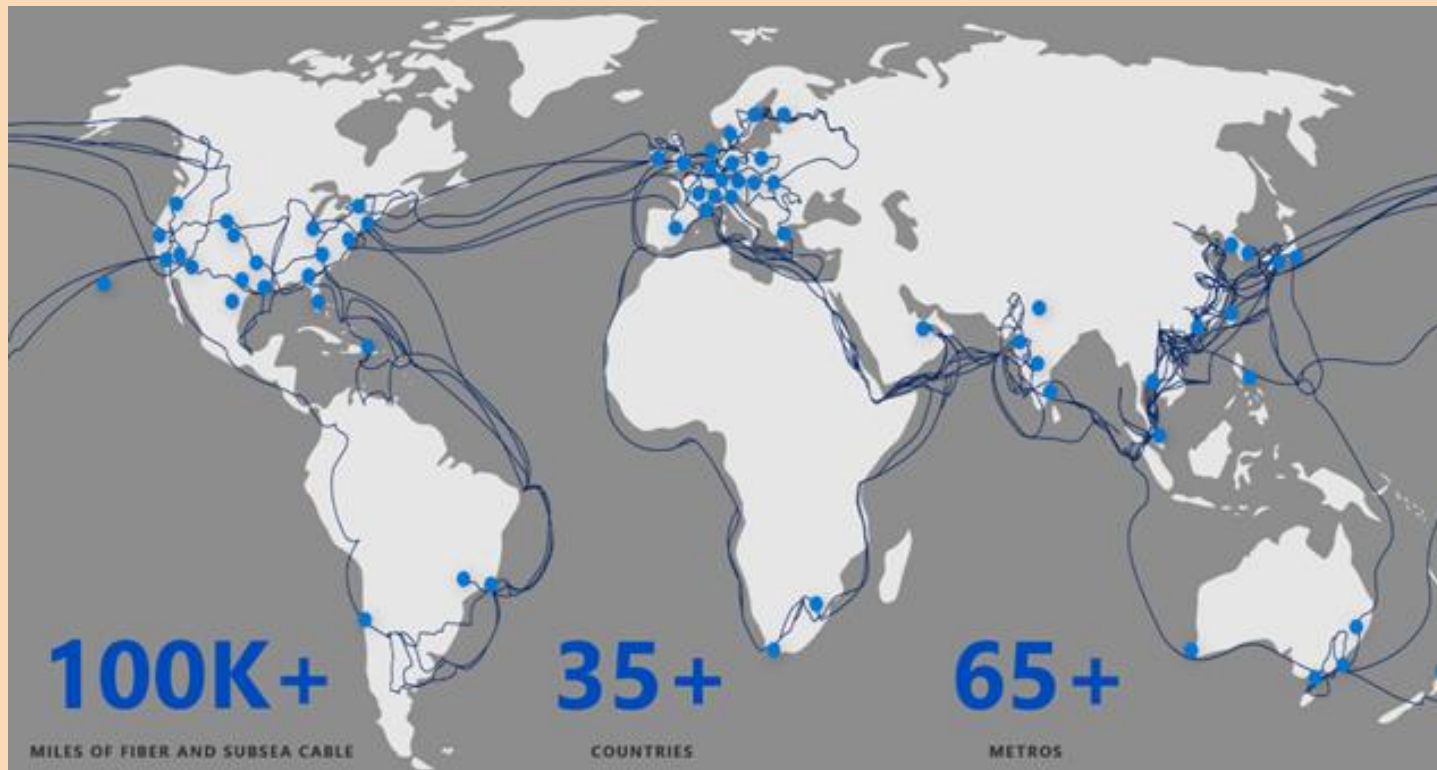
## How different islands of connectivity emerge and disappear



# Building a single manifold view

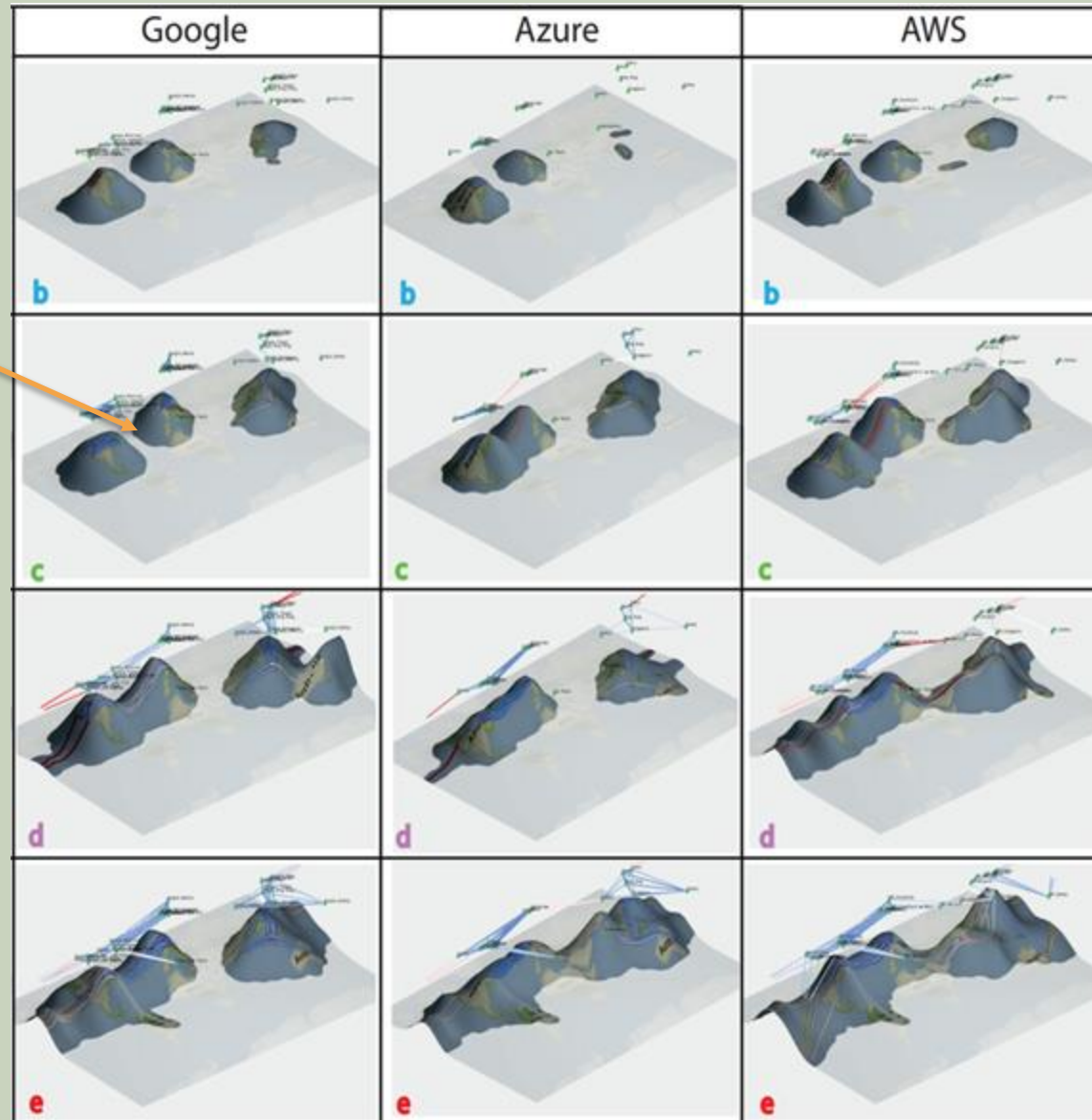


## Do we recover the cables according to Microsoft?



<https://www.microsoft.com/en-us/research/project/project-arno-cloudification-of-telecom-network-infrastructure/>

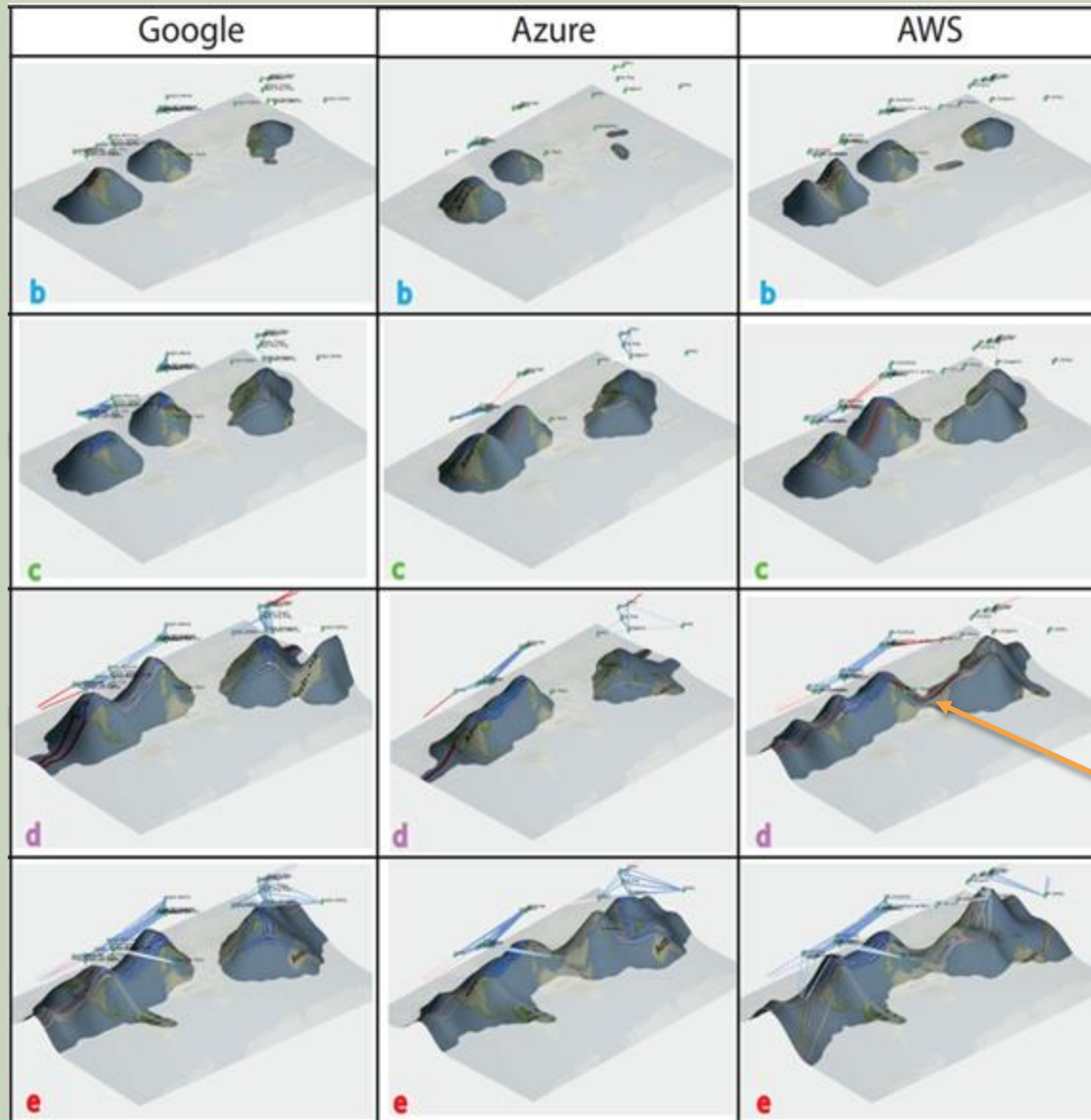
# Comparing cloud providers



Google has not  
percolated  
between Europe  
and US



# Comparing cloud providers



**AWS is the only cloud  
that has a direct path  
between Asia and  
Europe**

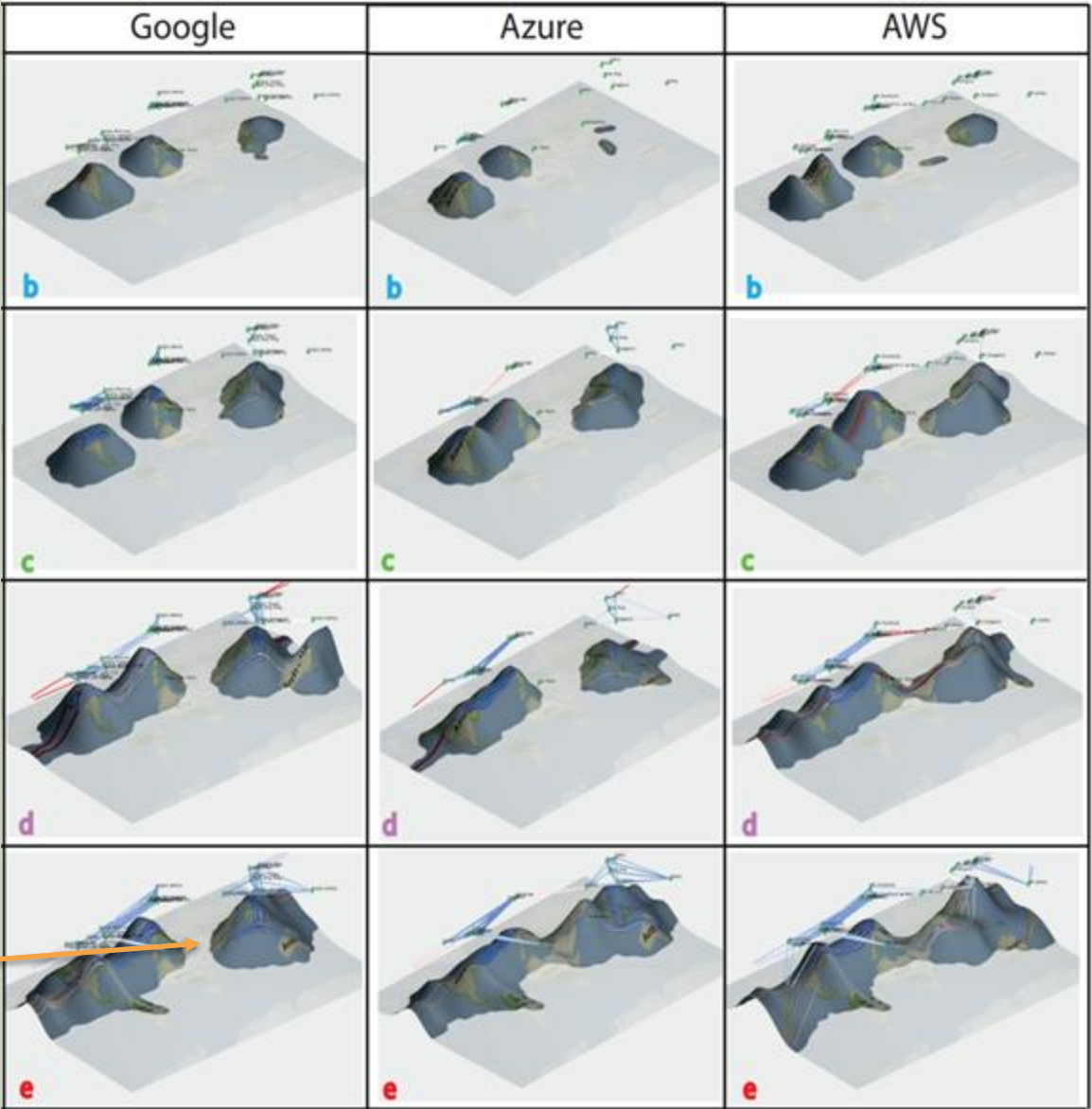
# Comparing cloud providers



Google has the most positive curvature between NA and EU



# Comparing cloud providers



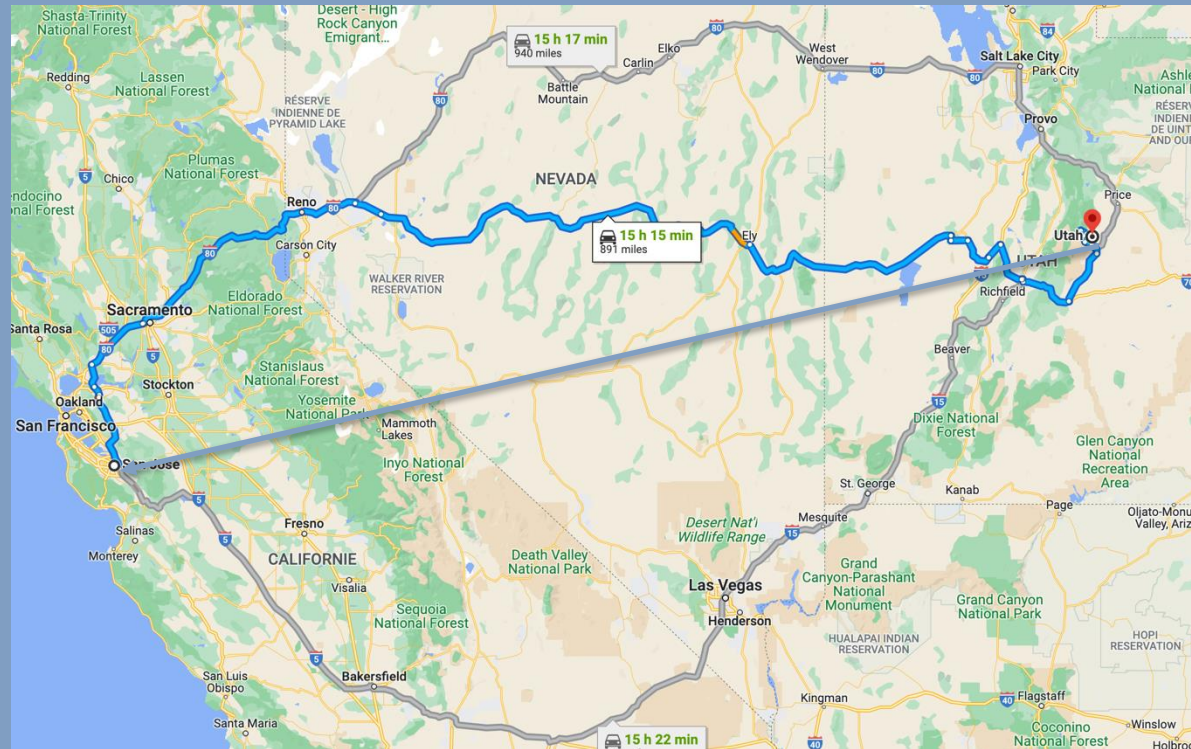
Google is not connecting Asia to Europe directly.

The geodesic on the manifold predicts the latency better than the great circle distance the GCD

Cloud	City A	City B	Latency	$\delta_{\text{GCD}}$	$\delta_{\text{Geo}}$	$d_{\text{RD}}$	$d_{\text{GCD}}$
Amazon	Sydney	Tokyo	104.6	-28.5	-1.2	10184	8147
	Ashburn	Sao Paulo	118.3	-12.2	3.0	9580	7664
	Dublin	Tokyo	202.0	39.0	-11.3	11980	9584
	Paris	Singapore	155.5	-27.0	-4.0	13415	10732
	Mumbai	Paris	104	-14.5	-6.0	8761	7009
Google	Osaka	London	221	55.4	5.7	12205	9499
	Mumbai	London	333	211.4	42.3	9247	7191
	Las Vegas	Sydney	142	-74.6	-48.7	16578	14320
	Seoul	Jakarta	106	14.5	40.2	6421	5293
	Portland	Frankfurt	124	-22.3	-42.4	9872	7834
Azure	Sydney	Tokyo	106.7	-26.3	-0.1	10184	8147
	Ashburn	Sao Paulo	117.8	-12.4	10.1	9580	7664
	Dublin	Tokyo	233.5	70.5	10.2	11980	9584
	Seoul	Amsterdam	220.5	75.7	25.6	11263	8516
	Singapore	Des-Moines	194.2	-59.5	-56.8	17872	14926

## Selecting route distance over great circle distance

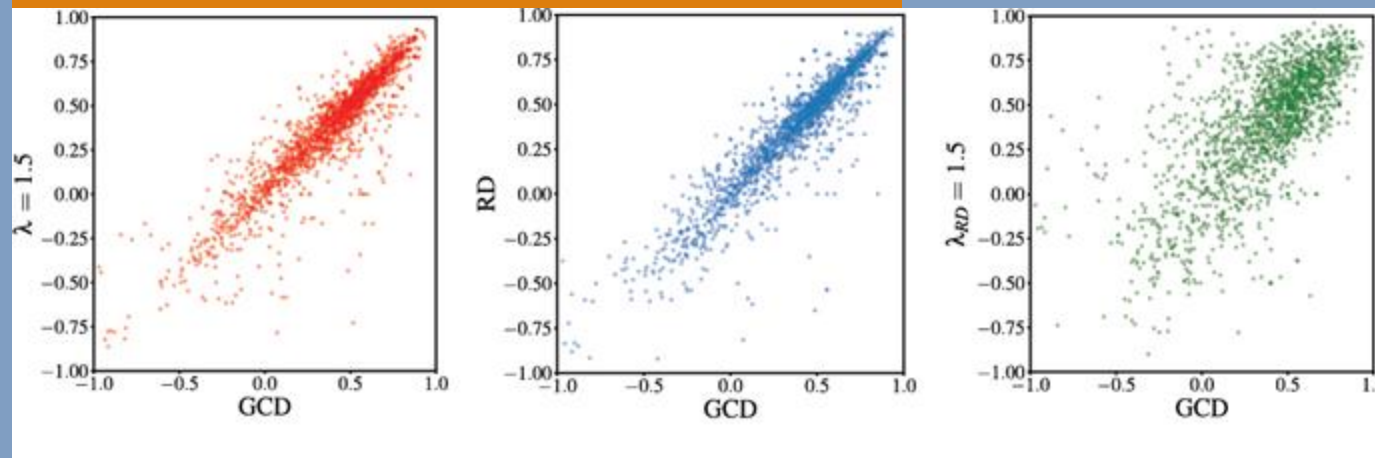
Right of way distance (or route distance) as a more appropriate metric to encapsulate topography



## Selecting routing distance over great circle distance

Right of way distance (or route distance) as a more appropriate metric to encapsulate topography

GCD is sufficient for our purpose



## Changing granularities

Selecting quotient over difference for remaining latency

Quotient is a good metric when identifying  
smaller scale patterns

## Changing granularities

### Selecting quotient over difference for remaining latency

Quotient is a good metric when identifying smaller scale patterns

### Selecting smaller time-windows

Changing time used for selecting the minRTT provides different view

## Alternative graph metrics

# Selecting Ricci curvature over different bottleneck metrics

Cut metric and betweenness centrality are not robust metrics.

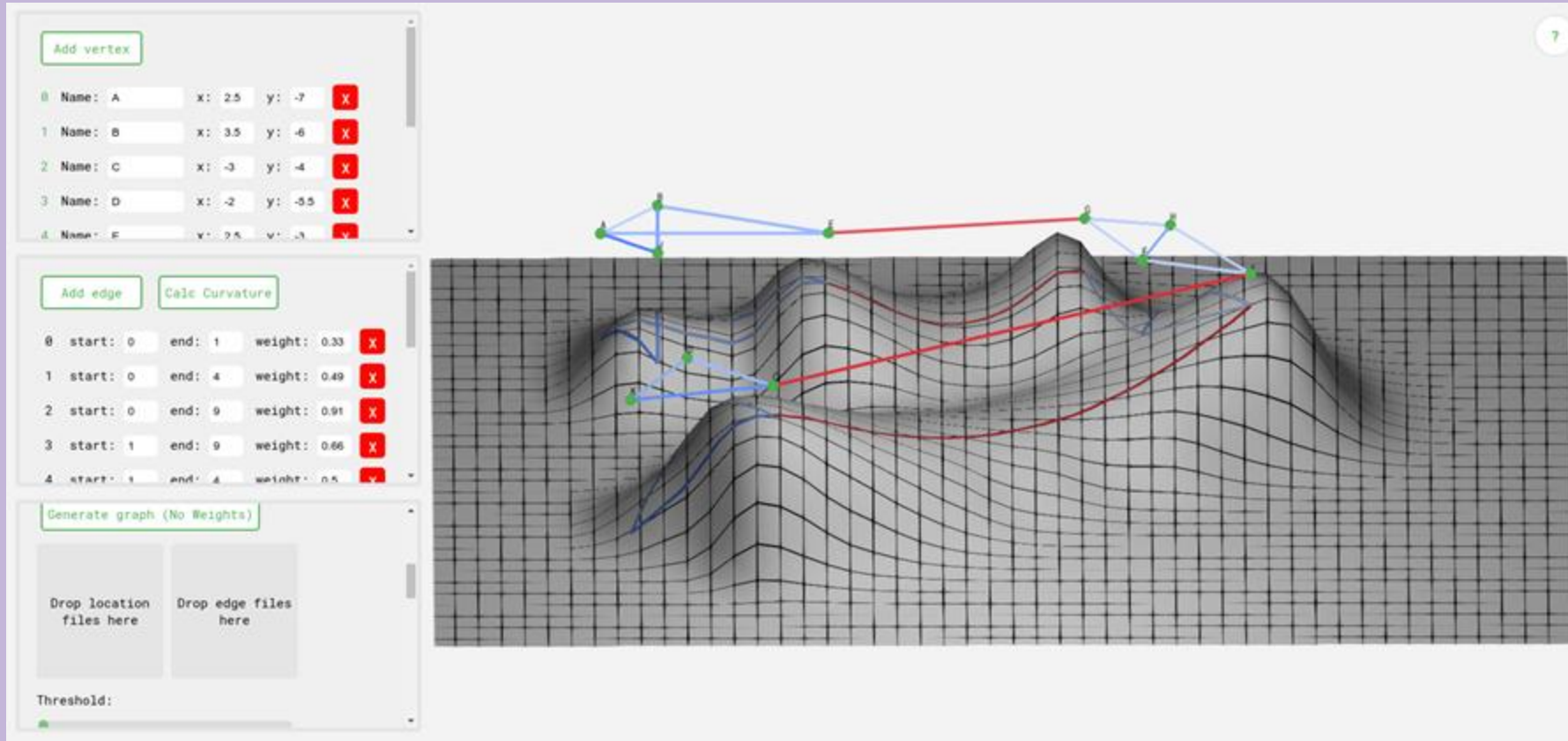
*Lemma:*

The maximal change in the  $L^1$  of the Ricci curvature distribution that the addition or deletion of an edge can induce is 6.



# Future steps

Sharing the manifold visualization tool and keep on improving its outputs

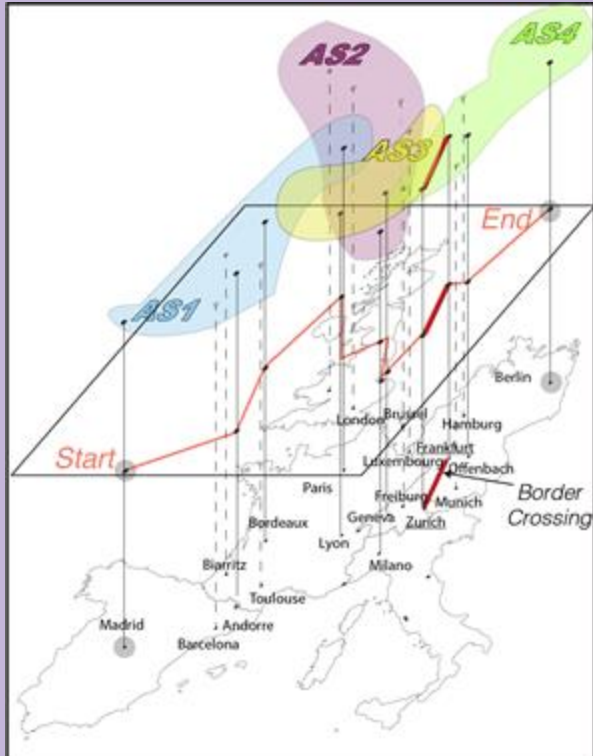




# Future steps

Sharing the manifold visualization tool and keep on improving its outputs

Applying the technique for Public Internet



***Routing is way harder for public Internet***

# Conclusions

In this presentation, we have:

1. introduced a new technique to uncover topology that was based on Riemannian geometry.

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***Questions?***